# ClassPad Advanced Skills

#### Main

M1. Use Shift Key shortcuts.



M2. Combine, expand, factor and simplify: use Transformation/combine - factor - simplify

(a) Combine 
$$\frac{x+1}{2-x} + \frac{2x}{11}$$

(b) Simplify 
$$(x + y)^2 - (x - y)^2$$

M3. Define your own functions: use Interactive/Define

(Use 'abc' tab to enter function name)

(a) 
$$f(x) = (2x^2 + 3x)(7x - x^2)$$

M4. Differentiate and integrate: use Calculation/diff - \$\infty\$

(a) 
$$\frac{d}{dx}(2x^2+3x)(7x-x^2)$$

(b) 
$$\frac{d}{dx} \left( \frac{x^2 - 7}{2x + 3} \right)$$

(c) 
$$\int x(5-3x^2)^3 dx$$

M5. Implicit differentiate: use Calculation/Impdiff

(a) 
$$x^3y^2 - 2xy = 5$$

**M6**. Find gradient and equation of tangent to  $y = \frac{x^2 - 7}{2x + 3}$  at (1, -1.2): use Calculation, tanLine

M7. Solve equations: use Advanced/solve

(a) 
$$\frac{x+1}{2-x} + \frac{2x}{11} \ge 4x$$

**M8**. Solve for x, y and z the equations 2x+3y-z=8, 3x-1=4y+3z and 3y=4x-2z+2

M9. Calculate probabilities using normal distribution: use Distribution, normCDf - Inv. Distribution, invNormCDf If  $X \sim N(62,14^2)$  then find (a) P(X < 50) (b) P(65 < X < 75)

(c) k, if P(X > k) = 0.1

M10. Calculate probabilities using Binomial distribution: use Distribution, binomialPDf or binomial CDf or Inv. Distribution, invBinomialCDf

If 
$$X \sim B(8, 0.4)$$
 then find (a)  $P(X \le 3)$ 

(b) 
$$P(4 < X < 7)$$

(b) 
$$P(4 \le X \le 7)$$
 (c) k, if  $P(X \le k) \ge 0.9$ 

M11. Use absolute value and counting technique InPrincr tools.

(a) 
$$\int_{-1}^{3} |x^2 - 4| dx$$

(b) 
$${}^{50}C_4$$
 .

M12. Use vector and matrix menus:

(a) Find angle between 
$$\begin{bmatrix} 1 \\ -2 \end{bmatrix}$$
 and  $\begin{bmatrix} 3 \\ 2 \end{bmatrix}$ .

M13. Use fMax and fMin to find global min and max for a function: Interactive, Calculation, fMax - fMin

(a) Find min and max value of  $x^3 - 4x^2 - x + 4$  between x = -1 and x = 5.

## **eActivity**

E1. Normal probabilities: Use (3AB) Normal prob

(a) If 
$$X \sim N(62,14^2)$$
 then find k, if  $P(57 < X < k) = 0.3$ 

(b) Find m if 
$$X \sim (m,8)$$
 and  $P(X > 33) = 0.75$ 

E2. Trapped area between two functions: Use (3CD) Area between curve

Find the area trapped between  $y = x^2 - 4x + 2$  and y = x - 2.

**E3**. Ship A is at −12**i**+25**j** km and wants to intercept Ship B at 10**i**−8**j** km and travelling with velocity 7**i**+24**j** km/h. If A has a speed of 30 km/h, find its velocity vector to intercept B and time taken.

#### **Finance**

Compound interest problems: Loan \$30000. Rate 6.6%pa. Monthly repayment \$600.

- (a) How long to repay? Last repayment? Total interest?
- (b) Repay in 3 years. Repayment?

### **Graph and Table**

GT1. Set a graph background and model curve: Tap Diamond to left of Analysis...

**GT2**. Find equation of tangent to  $y = 4x + 5 - x^2$  at (4,5): Analysis, Sketch, Tangent menu.

**GT3**. Trapped area between two functions: *Use (3CD) Analysis, GSolve, Integral, Intersection* Find the area trapped between  $y = x^2 - 4x + 2$  and y = x - 2.

GT4. Use integral and volume of revolution: Analysis, G-Solve menu.

Find volume of revolution when the area between  $y = \sqrt[3]{x+3}$ , y = 0, x = 1 and x = 4 is rotated about the x-axis.

**GT5**. Draw the graph of  $f(x) = \frac{2}{x+1}$  and its inverse: *Analysis, Sketch, Inverse menu*.

#### **Statistics**

**ST1**. Calculate normal probabilities and view graphs: use Calc, Distribution, Normal CD - Inv. Distribution, Inverse Normal CD

If 
$$X \sim N(62,14^2)$$
 then find (a)  $P(65 < X < 75)$ 

(b) 
$$k$$
, if  $P(X > k) = 0.1$ 

**ST2**. Calculate Binomial probabilities and view graphs: use Calc, Distribution, Binomial PD or Binomial CD or Inv. Distribution, Inverse Binomial CD

If 
$$X \sim B(8, 0.4)$$
 then find (a)  $P(X \le 3)$ 

(b) 
$$P(4 \le X \le 7)$$

(c) 
$$k$$
, if  $P(X \le k) \ge 0.9$ 

**ST3**. Calculate a probability using Central Limit Theorem: *use Calc, Test, OneSampleZTest*Use the CLT to estimate the probability that a random sample of 30 items drawn from  $X \sim N(40, 5.5^2)$  will have a mean of at least 42.

ST4. Calculate a confidence interval: use Calc, Interval, One-Sample ZInt.

A population is normally distributed with a standard deviation of 8. Find 95% confidence interval for mean when (a) sample of size 40 has mean of 65 (b) sample drawn is 55, 60, 71, 57, 62, 59, 61, 52 and 66.

**ST5**. Calculate a HyperGeometric probability: *use Calc, Distribution, HyperGeometric CD* If 6 people are chosen at random from a class of 3 left-handed and 27 right-handed students, what is the probability that 2 or more of the 6 are left-handed?

**Spreadsheet** - remember two types of cell selection

**SS1.** Predict the sales (1000's kg) for March 1989 from the data shown.

# **Programs**

eg AP, GP, mav, repay, saving

Quarter	t	Sales
March 1986	1	2.1
June	2	1.6
September	3	3.0
December	4	3.1
March 1987	5	3.2
June	6	2.2
September	7	4.0
December	8	4.1
March 1988	9	4.1
June	10	3.0
September	11	5.5
December	12	5.7